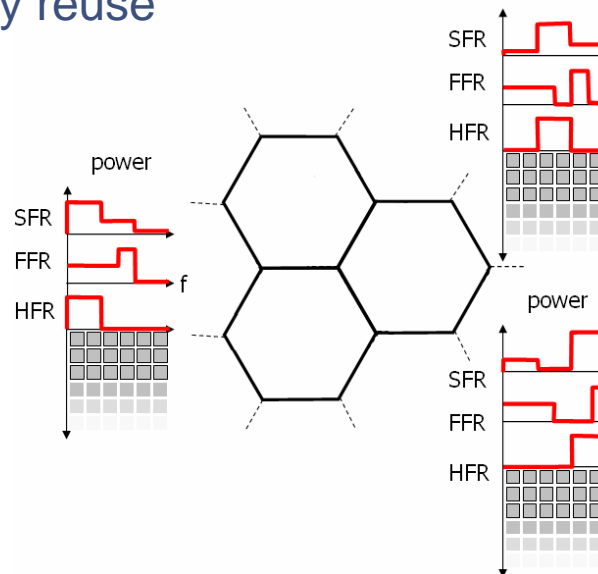




*Comments on the coupling of interference coordination
and resource allocation in OFDMA networks*

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VDE Fachgruppe 5.2.4 / Stuttgart
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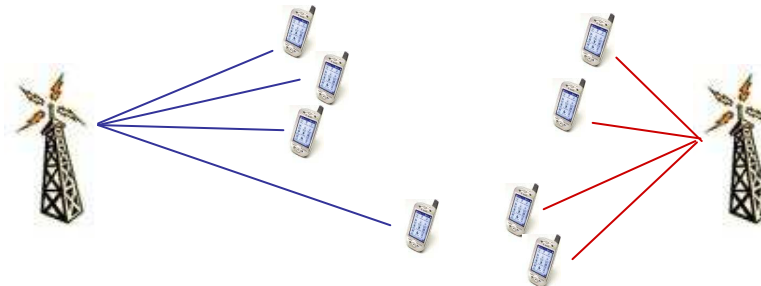
- Reuse 1 networks can benefit from power masking
- Different power mask concepts studied in the literature:
 - Hard frequency reuse
 - Fractional frequency reuse
 - Soft frequency reuse



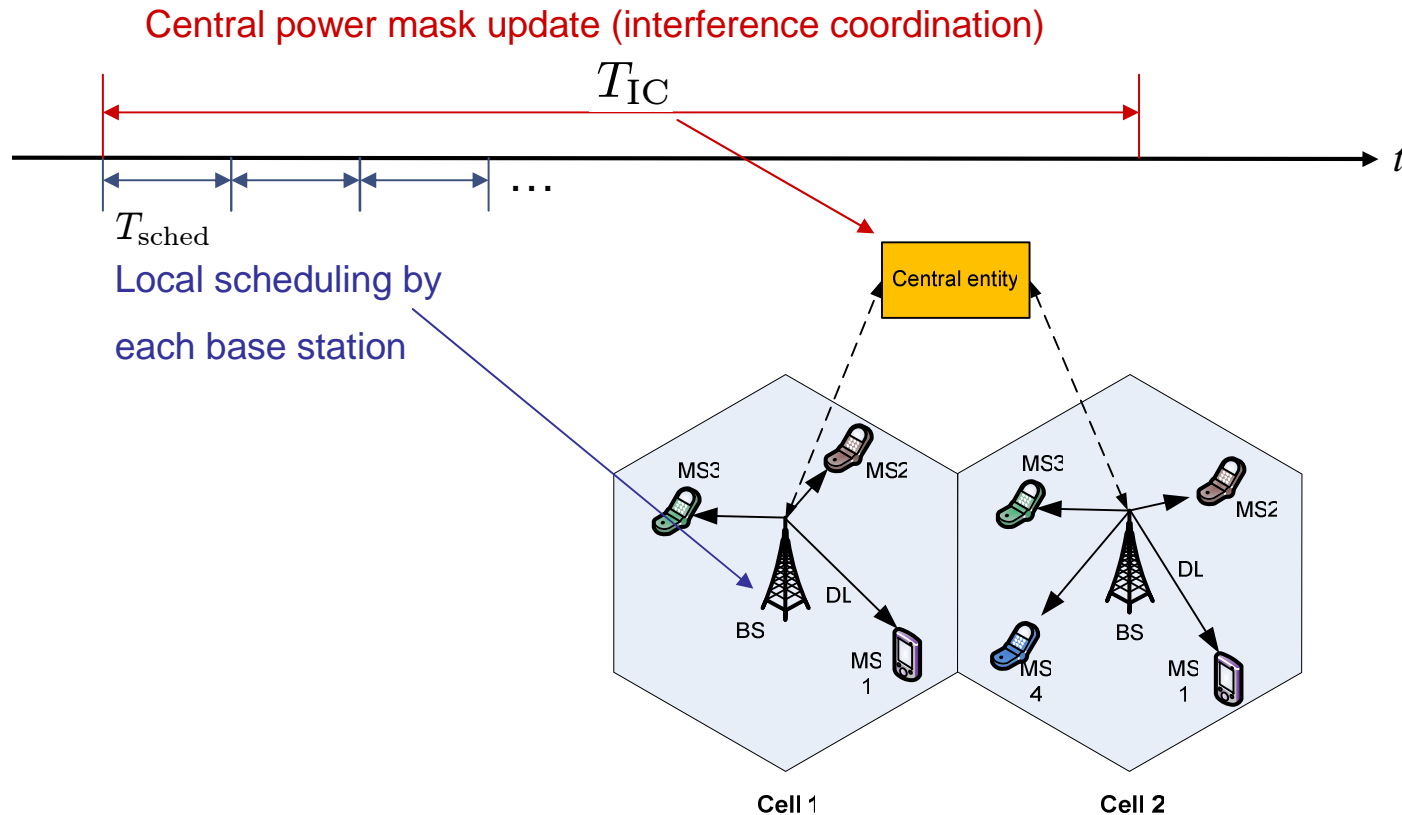
- Well known that FFR and SFR outperform HFR and flat power masks significantly

M. Bohge, J. Gross, A. Wolisz, "Optimal Power Masking in Soft Frequency Reuse based OFDMA Networks," in *Proc. of European Wireless Conference (EW'09)*, Alborg, Denmark, May 2009.

- However, static power masking (either FFR or SFR) is vulnerable to load imbalances in the cells
 - Concepts like adaptive soft frequency reuse currently discussed
 - Main idea: Update periodically the power masks according to load



- Within each period base stations perform local scheduling
- Contribution of this talk: Dependence between local scheduling and power masking
 - Do we need to account for the multi-user scheduling gain?
 - What should be guidelines?



- Mapping of instant. SINR to rate, i.e. $\mathcal{F}(\gamma) = \log_2(1 + \gamma) \cdot \gamma$
- Load: VoIP packet flows, maximum queueing delay of 50 ms
- Only considering the downlink in the following

- **BS performs local scheduling independently every T_{sched} :**
 - Power mask (power setting per RB from central entity)
 - Current channel state information (SINR feedback per RB)
 - Queue state
 - Objective: minimize the queuing delay by RB assignment

$$\max \quad \sum_j \sum_q y_{j,q} \cdot d_{j,q}$$

$$\text{s. t.} \quad \sum_n x_{j,n} \cdot \mathcal{F}(\gamma_{j,n}) \geq \sum_q y_{j,q} \cdot S_{j,q}, \quad \forall j$$

$$\sum_j x_{j,n} \leq 1, \quad \forall n$$

j : Terminal index

n : RB index

q : Packet index

γ : SINR

d : Packet delay

s : Packet size

x : RB assignment (0/1)

y : Packet assignment (0/1)

- **‘Central entity’ updates power masks for several cells every T_{IC}**
 - Power masks generated based on signal and interference gains
 - Objective: Maximize minimum rate among all terminals (for VoIP support)

$$\begin{aligned}
 & \max \quad \epsilon \\
 \text{s. t.} \quad & \sum_n x_{j,n,k} \cdot \mathbb{E} [\mathcal{F}(\gamma_{j,n,k})] \geq \epsilon, \quad \forall j, k \\
 & \sum_j x_{j,n,k} \leq 1, \quad \forall n, k \\
 & \sum_n p_{n,k} \leq P_{\max}, \quad \forall k
 \end{aligned}$$

j : Terminal index
 n : RB index
 k : Cell index
 γ : SINR
 P : Transmit power budget
 x : RB assignment
 p : Power assignment

- Note: Only power masks reported back to base stations

- What is a good expression for $E[\mathcal{F}(\gamma)] = E[\log_2(1 + \gamma)]$?

- Assume exponentially distributed signal and interference gains:

$$g^s \sim \text{Exp}\left(\frac{1}{\rho^s}\right) \quad g^i \sim \text{Exp}\left(\frac{1}{\rho^i}\right)$$

- Fixing transmit powers yields a new random variable as SINR:

$$\gamma = \frac{p^s \cdot g^s}{p^i \cdot g^i + \sigma^2}$$

- PDF $f_\gamma(y) = \left[\frac{\sigma^2}{P_I y + P_S} + \frac{P_I P_S}{(P_I y + P_S)^2} \right] \cdot e^{-\frac{\sigma^2}{P_S} y}$

- CDF $F_\gamma(y) = 1 - \frac{P_S}{P_I y + P_S} \cdot e^{-\frac{\sigma^2}{P_S} y}$

where $P_S = p^s \cdot \rho^s$ $P_I = p^i \cdot \rho^i$

F. Naghibi and J. Gross, "How bad is interference in IEEE 802.16e systems?," in *Proc. of the 16th European Wireless Conference (EW'10)*, Lucca, Italy, April 2010.

- **Naive evaluation**: simply divide average received power by average interference power

$$E[\mathcal{F}(\gamma)] = \log_2 \left(1 + \frac{P_S}{P_I + \sigma^2} \right)$$

- **Static evaluation**: Accounting for the true average of the ‘capacitated’ SINR r.v. yields instead:

$$E[\mathcal{F}(\gamma)] = \int_0^\infty \log_2(1 + \gamma) \cdot \left[\frac{\sigma^2}{P_I \cdot \gamma + P_S} + \frac{P_S \cdot P_I}{(P_I \cdot \gamma + P_S)^2} \right] \cdot e^{-\frac{\sigma^2 \cdot \gamma}{P_S}} d\gamma$$

- **However, base stations are performing dynamic resource allocation !**

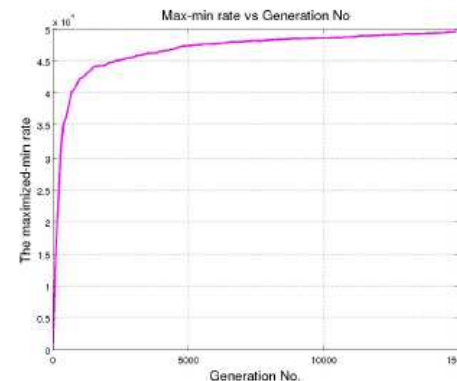
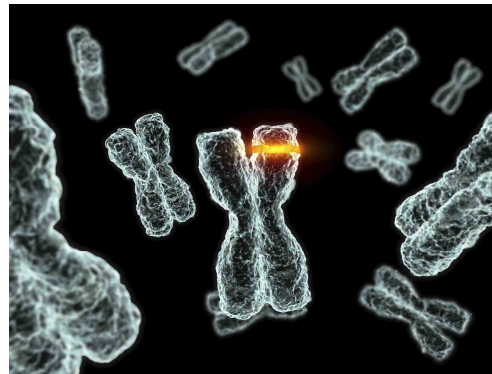
- **How to account for multiuser scheduling gain?**
 - Typical resource blocks assigned by local scheduling are much better than represented by the ,static‘ SINR r.v.
 - Use order statistics to account for scheduling gain:

$$E[\mathcal{F}(\gamma)] = \int_0^\infty \log_2(1 + \gamma) \cdot A \left[1 - \frac{P_S}{P_I \cdot \gamma + P_S} \cdot e^{-\frac{\sigma^2 \cdot \gamma}{P_S}} \right]^{A-1} \cdot \left[\frac{\sigma^2}{P_I \cdot \gamma + P_S} + \frac{P_S \cdot P_I}{(P_I \cdot \gamma + P_S)^2} \right] \cdot e^{-\frac{\sigma^2 \cdot \gamma}{P_S}} d\gamma$$

- Parameter to control: A
- Refer to this as dynamic evaluation

J. Gross, "Admission Control based on OFDMA Channel Transformation," in *Proc. of 10th IEEE International Symposium on a World of Wireless, Mobile and Multimedia Networks (WoWMoM)*, Kos, Greece, June 2009.

- Recall the power mask optimization problem: gets quite complex with above expression for expected capacity!
- Power masks are computed by genetic algorithm



- Optimization variables (power masks and resource block assignments) taken as chromosome:
 - Then repeat the cycle (= 1 generation):
Selection → Crossover and Mutation → Correction → Evaluation
 - Best chromosomes of previous phase taken as input for next power mask generation

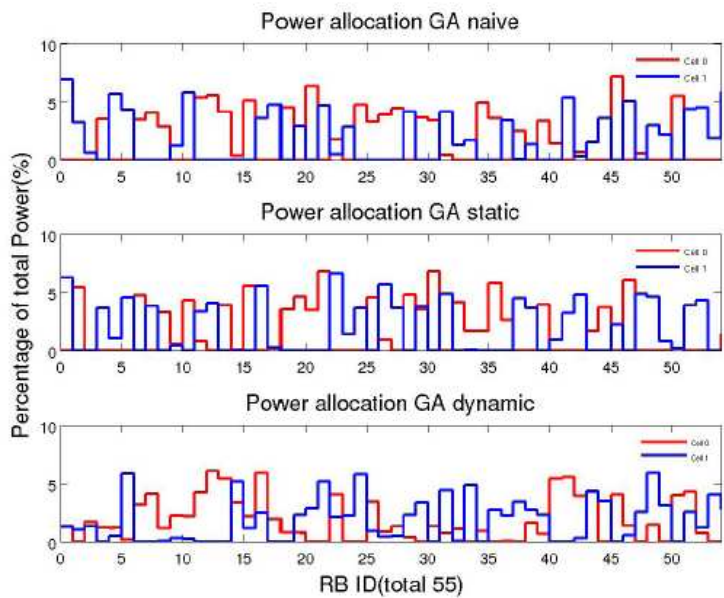
Evaluate performance by simulations

- Parameter:
 - 2 cell scenario (only one sector), 600 terminals
 - VoIP packet size 288 bits, IAT of 20 ms per flow
 - Local scheduling every 1 ms
 - Power mask update every 100 ms
 - Equal path loss/shadowing/fading model for all terminals
 - Packet dropping threshold: 50 ms

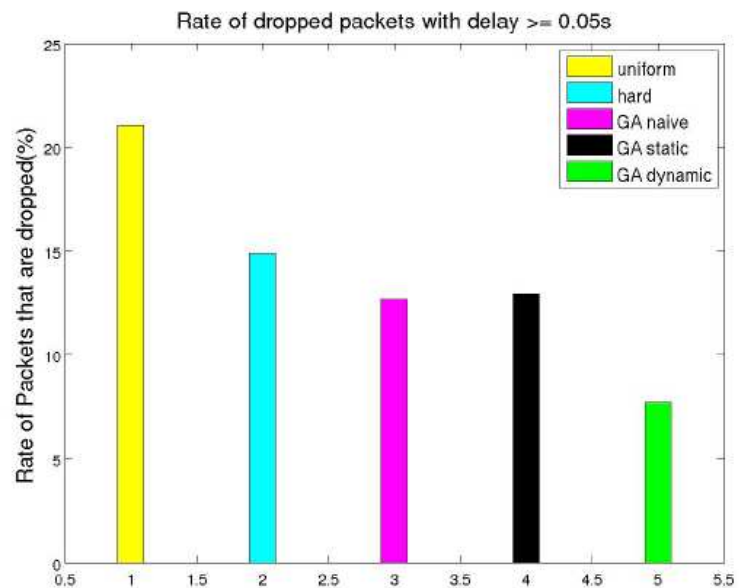
- Metrics:
 - Average drop rate
 - ECDF of the packet delay

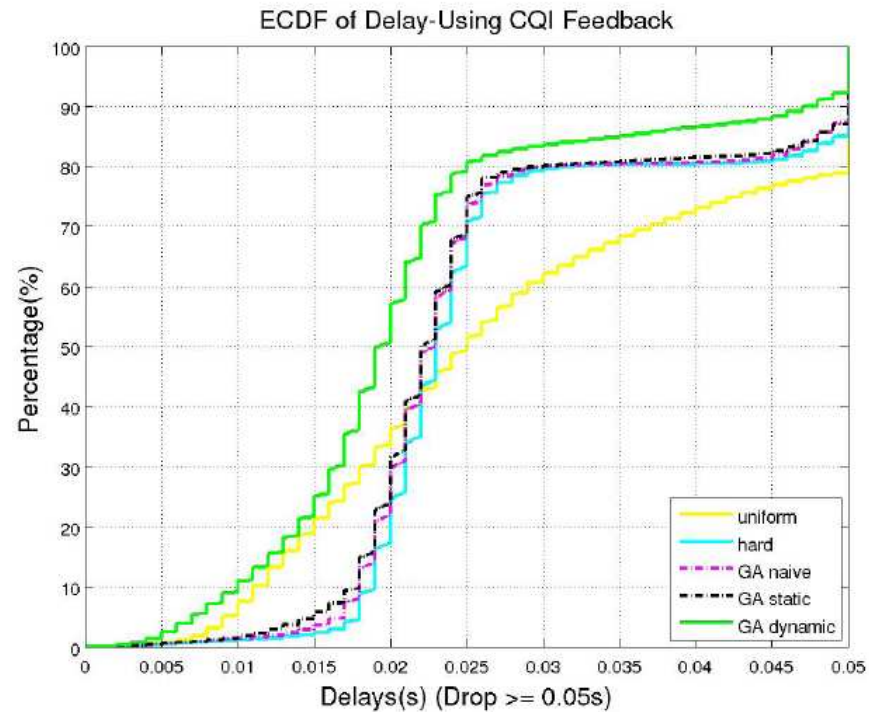
- Compared schemes:
 - Uniform power mask
 - Reuse 2
 - Adaptive power mask (naive, static, dynamic)

Power masks



Packet drop rate





~ 50 more VoIP clients supported if scheduling gain taken into account!

- **Accounting for multi-user diversity scheduling in interference coordination is crucial!**
 - Otherwise, no gain seen from interference coordination!
 - Is there a correct way of coupling IC with resource allocation?
Order statistics is a candidate to do so ...
 - Not shown here: some performance dependency on the factor A

- **Adaptive SFR can yield significant performance gain**
 - Work in progress:
 - Tune GA to get better results
 - Switch to scenario with more cells